

Digital Signal Processing

http://kom.aau.dk/~zt/courses/Digital_signal_processing/

Solutions 1 (MM1)

Exercise 1.1

$$\begin{array}{rcccccccc} x & = & 1 & -2 & 4 & 6 & -5 & 8 & 10 \\ n & = & -4 & -3 & -2 & -1 & 0 & 1 & 2 \end{array}$$

(a)

$$\begin{array}{rcccccccccccc} x1(n) & = & 3 & -6 & 10 & 22 & -23 & 12 & 41 & -18 & -16 & 6 & -5 & 8 & 10 \\ n & = & -6 & -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{array}$$

(b)

$$\begin{array}{rcccccccc} x2(n) & = & 0 & 8 & -20 & 0 & -50 & 64 & -50 & 0 \\ n & = & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 \end{array}$$

Exercise 1.2

$$T_1[x(n)] = \sum_{k=0}^n x(k)$$

(a) Not stable: $x(k) = M$, $T_1[x(n)] = (n+1) \cdot M$, As $n \rightarrow \infty, T_1 \rightarrow \infty$.

(b) Not causal: when n is smaller than 0, T_1 depends on future values of x .

(c) Linear: $T_1[ax_1(n) + bx_2(n)] = aT_1[x_1(n)] + bT_1[x_2(n)]$

(d) Not time-invariant: $T_1[x_1(n)] = \sum_0^n x_1(k) = \sum_0^n x(k - n_0) \neq y_1(n) = y(n - n_0) = \sum_0^{n-n_0} x(k)$

$$T_2[x(n)] = \sum_{k=n-10}^{n+10} x(k)$$

(a) Stable: $x(k) \leq M$, $T_2[x(n)] \leq 21 \cdot M$.

(b) Not causal: refer to future values.

(c) Linear: as in 1.2 (c).

(d) Time-invariant: $T_2[x_1(n)] = \sum_{n-10}^{n+10} x(k - n_0) = y_1(n) = y(n - n_0) = \sum_{n-n_0-10}^{n-n_0+10} x(k)$

Exercise 1.3

$$y[n] = \delta[n] + \frac{1}{2}\delta[n-1] + \frac{1}{2}\delta[n-2] - \frac{1}{2}\delta[n-3]$$